Non-Poissonian Quantum Jumps of a Fluxonium Qubit due to Quasiparticle Excitations

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As the energy relaxation time of superconducting qubits steadily improves, nonequilibrium quasiparticle excitations above the superconducting gap emerge as an increasingly relevant limit for qubit coherence. We measure fluctuations in the number of quasiparticle excitations by continuously monitoring the spontaneous quantum jumps between the states of a fluxonium qubit, in conditions where relaxation is dominated by quasiparticle loss. Resolution on the scale of a single quasiparticle is obtained by performing quantum nondemolition projective measurements within a time interval much shorter than $T_1$, using a quantum-limited amplifier (Josephson parametric converter). The quantum jump statistics switches between the expected Poisson distribution and a non-Poissonian one, indicating large relative fluctuations in the quasiparticle population, on time scales varying from seconds to hours. This dynamics can be modified controllably by injecting quasiparticles or by seeding quasiparticle-trapping vortices by cooling down in a magnetic field.

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A mesoscopic superconducting circuit, of typical size smaller than 1 mm², cooled to a temperature well below the superconducting gap, should be completely free of thermal quasiparticle (QP) excitations. However, in the last decade, there has been growing experimental evidence that the QP density at low temperatures saturates to values orders of magnitude above the value expected at thermal equilibrium [1–5]. These nonequilibrium QP excitations limit the performance of a variety of superconducting devices, such as single-electron turnstiles [6], kinetic inductance [7,8], and quantum capacitance [9] detectors, microcoolers [10,11], as well as Andreev bound state nanosystems [12,13]. Moreover, QPs are an important intrinsic decoherence mechanism for superconducting two level systems (qubits) [14–19]. In particular, a recent experiment performed on the fluxonium qubit showed energy relaxation times in excess of 1 ms, limited by QPs [20]. Surprisingly, the sources generating these QP excitations are not yet positively identified. The measurement of nonequilibrium QP dynamics at low temperatures could provide insight into their origin as well as an efficient tool to quantify QP suppression solutions.

In this Letter, we show that the quantum jumps [21] of a qubit whose lifetime is limited by QP tunneling, such as the fluxonium artificial atom, can serve as a sensitive probe of QP dynamics. A jump in the state of the qubit indicates an interaction of the qubit with a QP, and therefore, fluctuations in the rate of quantum jumps are directly linked to changes in QP number. Tracking the state of the qubit in real time requires fast, single-shot projective measurement with minimal added noise, made possible by the advent of quantum-limited amplifiers [22–24]. In this work, we use a Josephson parametric converter (JPC) quantum-limited amplifier [23,25] to monitor the state of our qubit with a resolution of 5 μs, 2 orders of magnitude faster than the qubit lifetime. We find that the qubit jump statistics fluctuates between Poissonian and non-Poissonian, corresponding to a change in the QP number. Surprisingly, these fluctuations do not average over time scales ranging from seconds to hours. The quantum jumps we measure in this work are driven by a few QPs in the entire device at any given time. In a related work, the dynamics of a population of a few thousands of QPs is probed by $T_1$ measurements of a transmon qubit [26].

The fluxonium qubit [27] [Fig. 1(a)] consists of a Josephson junction shunted by a superinductor [28,29], which is itself an array of large Josephson junctions [30]. An optical image of the fluxonium sample coupled to its readout antenna is shown in Fig. 1(b). An applied external flux $\Phi_{\text{ext}}$ strongly affects the fluxonium spectrum, energy eigenstates, and its susceptibility to different loss mechanisms. The overall quality factor $Q$ of the fluxonium is given by

$$\frac{1}{Q} = \sum_x \eta_x \frac{p_x}{Q_x},$$

where $Q_x$ is the quality factor of the material involved in the loss mechanism $x$, $p_x$ is its participation ratio, and $\eta_x$ is the oscillator strength of the qubit transition induced by $x$. Figure 1(c) shows $\eta_x$ as a function of external flux for three main loss mechanisms—capacitive, inductive, and QP tunneling across the small junction. The main inductive loss mechanism for the fluxonium is due to QP tunneling across the array junctions. Note that around $\Phi_{\text{ext}} = \Phi_0/2$, the fluxonium qubit becomes insensitive to loss due to QP
FIG. 1 (color online). The fluxonium qubit. (a) Electrical circuit schematic. The small junction, which is modeled by an ideal tunnel junction (green) in parallel with a capacitor (red), is shunted by an array of large Josephson junctions (blue). (b) Optical microscope image of the fluxonium qubit inductively coupled to the antenna. The top and bottom insets show magnified images of the fluxonium loop and antenna pads, respectively. The small junction is shunted by a superinductance composed of an array of 95 Josephson junctions, enclosing a magnetic flux \( \Phi_{\text{ext}} \). (c) The oscillator strength \( \eta \) [see Eq. (1)] of different qubit decay mechanisms vs the applied external flux \( \Phi_{\text{ext}} \). The corresponding capacitive, inductive, and Josephson energies, defined for the fluxonium artificial atom in Ref. [27], are shown as \( E_C, E_L, \) and \( E_J \), respectively.

Uncorrelated quantum jumps obey Poisson statistics, leading to an exponential distribution of the time spent in the ground or excited state \( p(\tau) = (1/\bar{\tau})e^{-\tau/\bar{\tau}} \), where \( \bar{\tau} \) is the mean time spent in the ground or excited state. To enhance the visibility of deviations from Poisson statistics, which would merely show up as a nonexponential decrease of \( p(\tau) \), we depict the distribution \( \tau p(\tau) \) instead. In Figs. 3(a) and 3(b), we show two different second-long measurements of \( \tau p(\tau) \) distributions for the ground (blue) and excited (red) states, histogrammed with logarithmic bins. The dashed lines correspond to the distribution predicted by Poisson statistics with \( \bar{\tau} \) taken as the measured average time either in the ground (blue) or excited (red) state (see the Supplemental Material [31] for a detailed definition). There is significant deviation between the two measurements. In Fig. 3(b), we show a measurement record which we call quiet, apparently agreeing with Poisson statistics. The noisy record in Fig. 3(a) deviates significantly from the Poisson prediction, with long and short times appearing considerably more frequently than expected.

In Fig. 3(c), the mean time spent in the ground (blue) and excited (red) states is shown as a function of time, over several minutes. Each point corresponds to a 1 s temporal average. To quantify the deviation of each measurement from Poisson statistics, we calculate the fidelity of the measured histogram to the Poisson prediction \( F = \left( \sum_i \sqrt{M_i P_i} / \sum_i M_i \right) \), where \( M_i \) is the measured ground state histogram value of bin \( i \) and \( P_i \) is the predicted value of bin \( i \) for a Poisson process. In Fig. 3(d), we plot the deviation from Poisson statistics \( 1 - F \) corresponding to the measurements in Fig. 3(c). These two figures indicate a correlation between long fluxonium energy lifetimes and agreement with Poisson statistics [31]. The noisy seconds appear to have an abundance of short quantum jumps which distort the Poisson statistics, typical for the quiet seconds. Figure 3(e) shows \( \tilde{\sigma}_z \), the mean polarization of the fluxonium qubit for the same measurements. The fluctuations in polarization are not correlated with the fluctuations between quiet and noisy seconds. The examples in Figs. 3(a) and 3(b) were taken for measurements with.
Ground frequency of duration applying a microwave pulse resonant with the cavity cooling in a magnetic field.

We created a transient QP population in the array by reducing the number of QPs by cooling down our sample in a constant magnetic field corresponding to the ground state taken after the sample was cooled in pads [see Fig. 1(b)]. During the field cooldown process, the pads can trap vortices [32,33], which may act as QP traps due to the reduced superconducting gap in their cores [26,34–36].

We reduced the number of QPs by cooling down our sample in a constant magnetic field corresponding to \( \Phi_0/2 \) in the fluxonium loop. Under these conditions, the antenna pads [see Fig. 1(b)] are threaded by flux corresponding to several \( \Phi_0 \). During the field cooldown process, the pads can trap vortices [32,33], which may act as QP traps due to the reduced superconducting gap in their cores [26,34–36].

We created a transient QP population in the array by applying a microwave pulse resonant with the cavity frequency of duration \( t_G = 100 \mu s \) and amplitude of order 1 mV across the antenna, similarly to Ref. [26]. After a 5 \( \mu s \) wait for the cavity photons to leak out, we monitor quantum jumps for 10 ms, after which we repeat the cycle. We estimate that at least \( 10^6 \) QPs are generated during each pulse. In Figs. 4(a) and 4(b), we show a comparison between measurements of the mean time spent in the ground state without and with QP generation pulses. In the presence of QP generation pulses, the quiet seconds (higher mean time in the ground state) are suppressed [31].

We reduced the number of QPs by cooling down our sample in a constant magnetic field corresponding to \( \Phi_0/2 \) in the fluxonium loop. Under these conditions, the antenna pads [see Fig. 1(b)] are threaded by flux corresponding to several \( \Phi_0 \). During the field cooldown process, the pads can trap vortices [32,33], which may act as QP traps due to the reduced superconducting gap in their cores [26,34–36].

FIG. 2 (color online). (a) Circuit diagram of the measurement setup. The fluxonium qubit (green) is dispersively coupled to the readout cavity (orange) through the antenna [see Fig. 1(b)]. The readout signal reflected from the cavity is preamplified using a JPC; then, it is routed through a commercial high electron mobility transistor (HEMT) amplifier at 4 K and demodulated using a heterodyne interferometry setup at room temperature. (b) Histogram of measured \( I, Q \) quadratures for the fluxonium in equilibrium with its environment at \( \Phi_{\text{ext}} = \Phi_0/2 \). \( (\omega_p/2\pi = 665 \text{ MHz}) \). Each count corresponds to a 5 \( \mu s \) time interval of integration, and the total number of counts is 200,000. The two distinct peaks in the \( I, Q \) plane correspond to the ground (right) and first excited (left) states of the qubit. Their relative amplitudes give an effective temperature of 45 mK. (c) Three examples of measured quantum jump traces corresponding to the time evolution of the \( I \) quadrature for the same measurement presented in (b). We show the raw traces in blue and an estimate of the fluxonium qubit state calculated using a two-point filter (see the text) in orange. Note that the characteristic time between jumps is not constant throughout the record.

FIG. 3 (color online). Measurement of the quiet and noisy behavior of the fluxonium quantum jumps. (a),(b) Histograms with logarithmic binning of the time intervals between jumps \( \tau \) for the qubit in the ground (excited) [blue (red)] states, scaled by \( \tau \). Each count represents a 5 \( \mu s \) time interval. In dashed lines, we plot the Poissonian prediction with the measured mean time interval \( \bar{\tau} \). Each histogram was taken from a 1 s long measurement record. The insets show the corresponding linear binning histograms proportional to \( p (\tau) \). Data in (b) agree with the Poisson prediction, while in (a), they significantly deviate from it. (c) Measurement of the average time spent by the qubit in the ground (blue) and excited (red) states vs time. There are significant fluctuations in these values over the course of minutes. (d) \( 1 - F \) (see the text) vs time, quantifying the deviation between the measured histogram and the corresponding Poisson prediction for the ground state. (e) Average polarization of the fluxonium qubit vs time. The dashed blue line marks the average polarization, which corresponds to a temperature of 46 mK, and the gray dashed lines are markers for 40 and 60 mK. Note that the qubit temperature is not correlated with the fluctuations between the quiet and noisy intervals.
Taking advantage of the real time measurement of the qubit relaxation, we can monitor the time evolution of $\bar{t}$ after a QP generation pulse. In Fig. 4(d), we show the average time spent in the excited state before a jump to the ground state, as a function of time after the QP generation pulse for pulse length $t_G = 50 \mu s$. This yields the equilibration of qubit lifetime as injected QPs leave the junction array. The qubit lifetime eventually saturates to a steady state dominated either by nonthermal QPs or other loss mechanisms. The rate to jump from the excited to the ground state at time $t$ after the pulse is related to the relative QP density by \[ \Gamma_{e-g}(t) = x_{QP}(t) = \frac{2\Delta}{\hbar \omega_{ge}} 2\pi \frac{E_L}{\hbar} \] where $x_{QP}$ is the ratio of QPs to Cooper pairs in the junction and $\Delta$ is the superconducting gap. We fit the lifetime measurements to an exponential model $x_{QP}(t) = x_{QP} + [x_{QP}(0) - x_{QP}] e^{-t/\tau_{SS}}$ from which we extract the time to reach the QP steady state $\tau_{SS} = 125 \pm 25 \mu s$ and a non-thermal background QP density $\bar{x}_{QP} = 4 \pm 1 \times 10^{-8}$, corresponding to 1–2 QPs in the whole array. Note that the non-Poissonian jump statistics corresponding to the noisy seconds [see Fig. 3(a)] show fluctuations in the QP number on the order of their average value, also suggesting the presence of only a few QPs in the whole array. This value for $\bar{x}_{QP}$ is an order of magnitude lower than what was measured for the small junction in Ref. [20]. The origin of the difference is presently not understood, although one could speculate that QPs in the array more easily diffuse into the antenna. Note that the value for $\bar{x}_{QP}$ is neither correlated with the QP generation pulse length $t_G$ nor the time to reach the steady state $\tau_{SS}$ [see the inset of Fig. 4(d)]. The extracted $\bar{x}_{QP}$ should be treated as an upper bound, since contributions from other decay sources could be present. Because of the limited dynamic range of our qubit lifetime measurement, of only a factor of 4, we cannot distinguish between different QP removal mechanisms such as trapping, diffusion, or recombination [31]. The discrimination between these mechanisms was recently demonstrated in a transmon qubit [26].

From the quantum jump traces following a QP generation pulse, we can also extract the average polarization of the qubit and hence its effective temperature. In Fig. 4(e), we show the extracted temperature vs time, starting from 1.4 ms after a QP generation pulse, when the QP population has already saturated. The initial increase in temperature following the QP generation pulse is proportional to the pulse length $t_G$, and it is consistent with an estimated dissipated power of $10^{-10}$ W absorbed in the volume of the sapphire substrate. The temperature equilibration time $\tau_{eq}$ of several ms is much slower than the sapphire thermalization time and is likely limited by the sapphire-copper contact [31].

In conclusion, the distribution of spontaneous quantum jumps of a fluxonium qubit indicates large relative fluctuations in the energy lifetime of this artificial atom. Corresponding changes of the QP density in the superinductor appear to be the natural explanation. This is supported, in particular, by the increased fluxonium energy lifetime in the presence of QP-trapping vortices, which also render the jump statistics Poissonian. The density of QPs extracted from the measurement does not appear to self-average over periods of seconds, minutes, and even hours. This suggests they originate from sources external to the sample, such as stray infrared [3,38] or higher energy radiation [5,39]. In addition, the fluxonium quantum jump statistics resolves a single QP on a $\mu s$ time scale, which could be a useful property for a low flux, low energy, particle counting detector.
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