

# A Concept for a Submillimeter-Wave Single-Photon Counter

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**Abstract**—We discuss the design for a submillimeter-wave photometer, using a combination of superconducting and single-electron devices, which would have high quantum efficiency, very low noise-equivalent powers, and eventually even sub-microsecond timing resolution. The absorption of above-gap photons occurs in a small strip of superconducting Al, whose normal-state resistance can be matched efficiently to an antenna of a higher gap (Nb) superconductor. The quasiparticles produced by photon absorption are then confined via Andreev reflection, and forced to tunnel through a small SIS tunnel junction. The tunneling time is much shorter than the known ( $> 10 \mu\text{s}$ ) quasiparticle recombination time, so collection efficiency will be high. The device sensitivity would be limited by the small subgap current in the high-quality Al/AlO<sub>x</sub>/Al tunnel junction at temperatures (100 mK) well below  $T_c$ . Scaling based on the larger junctions used in X-ray detector applications suggests that the total dark current can be  $< 0.1 \text{ pA}$ , or of order  $10^5$  electrons/second, corresponding to an NEP of less than  $10^{-19} \text{ W}/\sqrt{\text{Hz}}$  at 500 microns (600 GHz). The photocurrent will be measured using a fast single-electron transistor (RF-SET), which allows a shot-noise-limited performance even for the very small currents delivered from this low capacitance and high impedance SIS junction. Results of initial fabrication and dc characterization of an integrated photodetector are also given.

## I. INTRODUCTION

How sensitive a direct detector does one need at submillimeter wavelengths? Heterodyne detectors (mixers) have in recent years achieved near quantum-limited performance [1] and are used for high resolution ( $\delta\nu/\nu \sim 10^{-6}$ ) astronomical observations, while direct detectors are generally preferred for wide bandwidth applications. A heterodyne system is limited by its fundamental quantum noise ( $1/2$  a photon per mode) when background temperatures are less than  $T_Q = h\nu/2k_b$  ( $\sim 25 \text{ K}$  @  $1 \text{ THz}$ ), while an ideal direct detector is limited only by fluctuations in the photon background impinging on the device. For wideband (of order octave) observations from even the best ground-based sites, this background limit due to atmospheric emission [2] corresponds to noise-equivalent

powers (NEP's) of about  $10^{-15}$  or  $10^{-16}$  watts. Cryogenic bolometers (for a review, see [3]), when operated below 0.3 K, can have sufficient sensitivity to easily reach this limit. Indeed, semiconductor detectors [4] now achieve sensitivities of  $10^{-17} \text{ W}/\sqrt{\text{Hz}}$ .

However, there are also applications in extragalactic astronomy in which require medium resolution ( $10^{-3} - 10^{-4}$ ) within some much wider total bandwidth and would be awkward to address using heterodyne instruments. Since the bandwidth is limited, ground flux is reduced, and detector sensitivity must be correspondingly higher [5],  $\leq 10^{-18} \text{ W}/\sqrt{\text{Hz}}$ . In addition, more, future space missions [6] with cooled optical spectral resolution might require drastically lower noise levels [7], approaching even  $10^{-21} \text{ W}/\sqrt{\text{Hz}}$ . The direct detector is of course a true photon counter and is always background-limited when the number of photons per second exceeds whatever "dark" counts the detector registers in the absence of light. While good photon counters exist (e.g., photomultipliers) at shorter wavelengths, no device has yet approached this goal in the submillimeter.

In the past few years, several novel bolometer structures and/or readout schemes have been developed that can address this range of sensitivities. Bolometers can use a voltage-biased superconducting transition junction (TES) combined with a SQUID readout, for which have demonstrated [8] electrical NEP's of  $10^{-17} \text{ W}/\sqrt{\text{Hz}}$  and have even been used for detection of individual optical and near-IR photons [9]. Another promising approach for achieving these very high sensitivities is the "NIS" microbolometer [10], in which an antenna-coupled normal metal strip is used as the absorber, and the readout temperature is readout using a normal-superconductor tunnel junction. These NIS bolometers have demonstrated electrical NEP's of a few  $10^{-18} \text{ W}/\sqrt{\text{Hz}}$ , and the predicted performance at 100 microns is of the order of  $10^{-19} \text{ W}/\sqrt{\text{Hz}}$ . An exciting superconductor technology for single-photon detection are superconducting tunnel junction (STJ) detectors, where the photon pulse in a superconductor-insulator-superconductor junction, due to the breaking of many Cooper-pair bonds by photon absorption in one of the electrodes, can be used for determination of photon energy. These STJ detectors have been used for spectroscopy of individual photons [11] down to near-IR [12] wavelengths.

In this paper, we introduce a device, called

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Quasiparticle Photon Counter (SQPC) for convenience, which combines demonstrated elements of both superconducting and single-electron (SET) technologies to produce a direct-detector with expected sensitivities of  $10^{-20}$   $W/\sqrt{Hz}$  or better. It is not a bolometer, but rather a non-equilibrium device which would first be operated as a photoconductor, but might eventually produce a true single-photon counter at submillimeter wavelengths with sub-microsecond speed and high quantum efficiency. Furthermore, the detector has an integrated readout scheme which has low power dissipation, small size, and a potential for multiplexing to produce large scale arrays. We first present the device configuration and basic operating principles, then discuss the dynamics of the response to a photon absorption, address the expected noise sources in the system and their optimization, continue with initial results from fabrication and dc characterization of the first such devices, and discuss the prospect of performing true single-photon counting at submillimeter wavelengths.

## II. DEVICE CONCEPT AND GEOMETRY

The basic configuration of the SQPC device is shown in Figure 1. A small strip of Al is connected to the terminals of a planar antenna fabricated from a higher-gap superconductor, such as Nb or NbTiN. Photons in the frequency range between the gap frequencies of the Al and the antenna ( $\sim 100$ -700 GHz, for Al and Nb) which impinge on the antenna will break Cooper-pairs in the Al strip. The quasiparticles produced will be trapped within the Al absorber due to Andreev reflection, and either recombine or tunnel through the submicron-area  $Al/AlO_x/Al$  tunnel junction, located to one side of the absorber. The junction is of submicron area, so that its capacitance is small (fF), its normal-state resistance is high ( $k\Omega$ ), and its leakage current, when biased below the superconducting gap voltage, can be picoamps or less.

The photocurrent across the SIS detector junction is measured using a capacitively-coupled high-speed quantum electrometer, namely a radio-frequency single-electron transistor (RF-SET) [13], as a transimpedance amplifier. The RF-SET is also fabricated from ultrasmall Al tunnel junctions, and integrated on chip. The RF-SET is optimized for measuring signals from large impedance sources, and can attain bandwidths of over 100 MHz for small source capacitances. The SIS junction is biased through a cooled feedback resistor, with the current return provided through the absorber and antenna.

When photons are absorbed, the quasiparticles tunnel across the junction, causing an increase in the current, so that the device operates as a photoconductor. In this mode, a readout using a conventional field-effect transistor would probably be possible. Because the RF-SET is in fact capable of counting a pulse consisting of only a few electrons on microsecond timescales or faster, however, and because the expected dark currents of less than a picoamp correspond to electron-counting rates ( $f=I/e$ ) of less than  $10^6$  per second, one might eventually be able to resolve individual photon absorptions. Although of course a single pair-breaking photon event leads to the production of two quasiparticles, we refer to this integrated detector as a Single Quasiparticle Photon Counter,

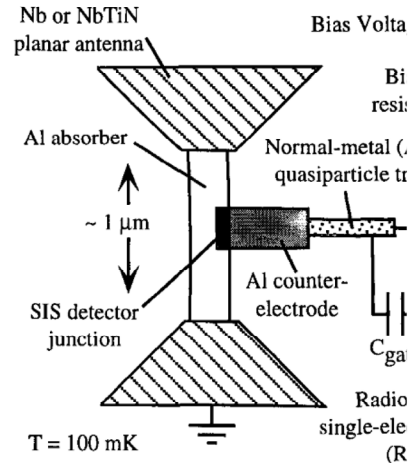


Fig. 1. Schematic layout of ultra-sensitive submillimeter detector and photon counter.

or SQPC.

Experts will recognize that this device is a STJ detector, carried to an extreme limit where photon charge pulses consist of only one electron, and utilizing antenna coupling rather than direct absorption. An SET has previously been used with a doped Si absorber to yield very low noise ( $W/\sqrt{Hz}$ ) at shorter wavelengths, but such devices have natural "bandgaps" of meV. Finally, single-photon counting by absorption directly in a superconductor, where a multiplication process gives a gain for each absorbed photon, was also discussed [15], although the issues of quantum efficiency and high-speed readout were not resolved.

## III. INPUT COUPLING, QUANTUM EFFICIENCY, AND RESPONSIVITY

In this device, the input coupling and readout can be separately optimized. The impedance of the Al absorber strip at frequencies well above the gap frequency approaches the normal state impedance. If the absorber impedance is impedance-matched to the antenna impedance, the incident power is absorbed by the Al strip, and the excess quasiparticles and high quantum efficiency for an absorber resistance of about 15 Ohms. The antenna impedance,  $Z_{ant} \sim 75$  Ohms, efficiency should be greater than 50% (in terms of the antenna). The use of a planar superconductor antenna also allows [16] low-loss tuning circuits to match the impedance, or the incorporation of filters to select the desired band for the detector.

If the photo-produced quasiparticles are collected, (see section on quasiparticle dynamics) then two quasiparticles are measured per photon. Note that this is twice the quantum efficiency of an ordinary SIS direct-detector [17] where two quasiparticles contribute to the tunnel current. When the photon energy exceeds the superconducting gap, the quantum efficiency is

pect the net result to be the production of 4 quasiparticles. Thus the number of quasiparticles produced per photon,  $2h\nu/2\Delta$ , scales as the photon energy, although with some discretization. The current responsivity is then approximately constant with frequency, with a value of  $e \times h\nu/\Delta/h\nu = e/\Delta$ , or about  $5 \times 10^3$  Amps/Watt for an aluminum absorber. However, the main advantage over an ordinary SIS direct-detector, where the radiation is coupled directly *across* the junction, is not responsivity. In the usual configuration, the conditions of efficient matching, which requires  $R_N$  of order the impedance of free space, and very low leakage current cannot be simultaneously met.

#### IV. QUASIPARTICLE DYNAMICS AND TIMESCALES

In order to preserve the efficient collection and measurement of the quasiparticles produced by the incident photons, we require a certain hierarchy of timescales within the detector, namely that the diffusion of the quasiparticles within the absorber, and their tunneling out through the SIS junction, should all take place on a timescale which is short compared to the recombination time. Even for absorber films with the resistivities of several  $\mu\Omega$ -cm that might be required to achieve a few ohms/square and efficient matching to the absorber, the diffusion constant should be in the range 1-10  $\text{cm}^2/\text{s}$ . This implies diffusion times,  $\tau_d = L^2/D$ , of 1-10 nanoseconds over the one  $\mu\text{m}$  absorber. Since the diffusion time is much shorter than the tunneling time out of the absorber, the quasiparticles will effectively sample the entire volume of the absorber, and the fraction of the absorber which is covered by the detector SIS junction is not important.

The time required for an individual quasiparticle to tunnel from the absorber simply depends on the product of the volume of the absorber and the normal state resistance of the tunnel junction. This process is identical to charge collection in shorter-wavelength STJ detectors, which is well understood [18]. The tunneling time,  $\tau_t$ , in the normal state is  $\tau_t = 2eR_N N_F V$ , where  $e$  is the electron's charge,  $R_N$  is the normal-state resistance of the junction,  $N_F$  is the density-of-states of the Al (per eV per volume), and  $V$  is the total volume of the absorber. In the superconducting case, with bias voltages much less than the gap, there are only small corrections of about a factor of two. For an absorber approximately  $1 \mu\text{m} \times 1 \mu\text{m} \times 200 \text{ \AA}$  thick, the volume is approximately  $10^{-14} \text{ cm}^3$ , and the tunneling time for a 10  $\text{k}\Omega$  junction would be about 1  $\mu\text{s}$ . We note that this is similar to the times found in X-ray STJ detectors; the Yale group [19] finds  $\tau_t \sim 1 \mu\text{s}$ , for an absorber volume about  $10^4$  times larger, and a resistance about  $10^4$  times smaller. If film thickness in the SQPC was decreased to 100  $\text{ \AA}$  and linewidth reduced to 0.2  $\mu\text{m}$ , the volume and hence the time could perhaps be an order of magnitude still smaller. One could further decrease the tunneling time by reducing the junction resistance, but this would come at the expense of an increased dark current and a decreased sensitivity (see next section). A normal-metal wiring layer (Au) is placed within a few microns of the detector junction counter-electrode. This helps to ensure that after tunneling, the quasiparticles diffuse away from the junction and are lost, before they have

TABLE I  
Device Parameters and Noise Sources for SQPC Detect

Device Parameters		
	Optimal Device	Init
Junction Resistance, $R_N$	10 $\text{k}\Omega$	
Dynamic Resistance, $R_d$	> 1 $\text{G}\Omega$	
Total Capacitance	1 fF	
Dark Current @ $V = 50\mu\text{V}$	< 50 fA	4
Electrons/second	< $3 \times 10^5$	3
Noise Sources		
Shot Noise ( $\text{A}/\sqrt{\text{Hz}}$ )	$1 \times 10^{-16}$	1
Johnson Noise ( $\text{A}/\sqrt{\text{Hz}}$ )	$1 \times 10^{-16}$	2.5
SET Charge Noise ( $\text{e}/\sqrt{\text{Hz}}$ )	$2 \times 10^{-6}$	5
SET Voltage Noise ( $\text{V}/\sqrt{\text{Hz}}$ )	$6 \times 10^{-10}$	1.5
Effective Current Noise [20] of SET ( $\text{A}/\sqrt{\text{Hz}}$ )	< $10^{-18}$	1.5
Readout Bandwidth	> 10 MHz	
Responsivity ( $\text{e}/\Delta$ )	5,000 A/W	5.0
Predicted NEP ( $\text{W}/\sqrt{\text{Hz}}$ )	< $3 \times 10^{-20}$	3

an opportunity to tunnel back into the absorber

Very long recombination times,  $\tau_R$ , have been observed [21] in Al films at these low temp and times greater than 10  $\mu\text{s}$  are observed in devices. But for the very dirty, thin films such a absorber, the times will need to be determined. If less, we expect that the recombination time will be 1-2 orders of magnitude longer than the sub-mic tunneling time. So the desired hierarchy of timescales,  $\tau_d \ll \tau_t \ll \tau_R$ , should be well-satisfied, and there should be an efficient collection, with nearly all the quasiparticles produced by the photons resulting in excess current across the detector junction.

#### V. NOISE SOURCES AND DETECTOR SENSITIVITY

Since the SQPC will operate as either a photon detector or photon counter, the intrinsic limit on the detector sensitivity will ultimately be determined by the number of counts per second, or the leakage current of the detector junction. Again, a main advantage of the detector geometry we have chosen is that the detector junction resistance will be very high in resistance. Furthermore, the leakage current of Al/ $\text{AlO}_x$ /Al tunnel junctions in the subgap and at temperatures well below  $T_c$  can be a small fraction of the tunneling current in the normal state,  $V$  Al STJ devices operated at 0.25 K, subgap current times lower are commonly observed, and ratios of subgap to normal state conductance ratios can also be observed [22] below 0.1 K. Whether these ratios will have to be demonstrated. However, if a ratio can be obtained, then the leakage current of a junction with the very small area tunnel junctions of the detector will have to be demonstrated. However, if a ratio can be obtained, then the leakage current of a junction with a normal state resistance of 10  $\text{k}\Omega$ , when the gap is low, can be much less than a picoamp (1 pA). This corresponds to an electron counting rate of only  $10^5$  electrons per second. The minimum detectable photon flux in a 1 second integration would be the square-root of this number, or a few hundred photons per second, and is equivalent to NEP's of  $10^{-20} \text{ W}/\sqrt{\text{Hz}}$ .

The actual NEP of the detector, including

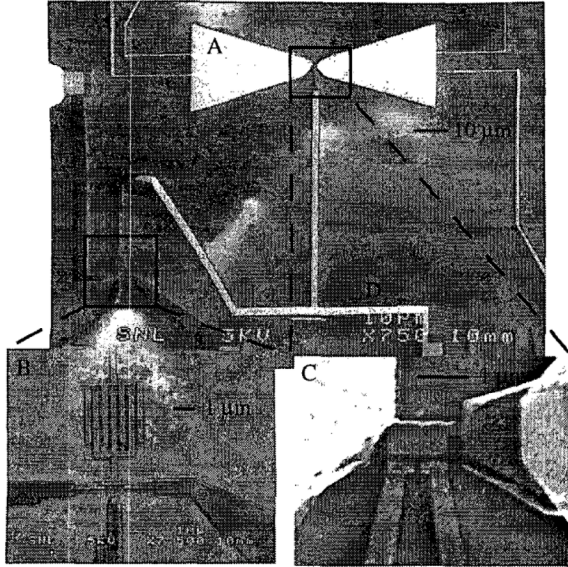


Fig. 2. SEM micrograph of completed photodetector, fabricated with multi-layer direct-write e-beam lithography. Shows A) chip layout including Pb bowtie antenna and Al absorber, B) integrated single-electron transistor with interdigitated finger capacitor, C) two SIS detector junctions with SQUID loop to allow suppression of critical current, and D) Au wiring/quasiparticle traps.

added in the readout, is determined by computing the total effective current noise (in Amps/ $\sqrt{\text{Hz}}$ ), and dividing by the responsivity,

$$NEP = \frac{i_n}{R} = (i_{shot}^2 + i_{johnson}^2 + |e_n/Z_{tot}|^2)^{1/2}/R, \quad (1)$$

where  $R$  is the responsivity (in Amps/Watt),  $i_{shot}^2$  is the shot noise of the dark current,  $2eI_{dark}$ ,  $i_{johnson}^2$  is the current noise of the bias resistor,  $4k_bT/R_b$ ,  $e_n$  is voltage noise of the SET  $e_n = q_n/C_{gate}$  ( $q_n$  is the charge noise of the SET), and  $Z_{tot}$  is the total impedance of load. This load impedance is equal to the parallel combination of the junction dynamic resistance,  $R_d$  and the total capacitance to ground of the node connected to the SET,  $C_{tot} = C_{junc} + C_{gate} + C_{parasitic}$ , so that  $Z_{tot} = R_d/(1 + j\omega R_d C_{tot})$ . The noise contribution of the SET therefore increases above the  $RC$  frequency of the load, and depends on the total capacitance. In the first design, we plan to use an off-chip, but cooled, feedback resistor, so  $C_{tot}$  will be a picofarad or more, at the expense of considerable bandwidth. With an on-chip resistor, perhaps even consisting another junction or a series array, the total capacitance can be maintained at only a few femtofarads. In the above we assume that  $i_n$  of the SET itself is negligible, since the gate resistance of this type of interdigitated capacitor on Si [23] is greater than  $10^{18} \Omega$ . The feedback resistors are assumed to have only Johnson noise, be cooled to 100 mK, and to have initial and final values of 100 and 250 M $\Omega$ , respectively.

Some representative numbers for both the device parameters and the terms contributing to the total NEP (Eq 1) are given in Table 1. In initial experiments, an ordinary SET, operated at low frequencies where  $1/f$  noise limits

the charge noise to several times  $10^{-5}$  elec be used. The RF-SET has demonstrated of about 15 micro-electrons/ $\sqrt{\text{Hz}}$  ( $1.5 \times 10$  simultaneous bandwidths of greater than simple design improvements are expected noise of only a few micro-electrons/ $\sqrt{\text{Hz}}$ . 'sitivity means that the readout can be fundamental shot noise of the leakage current bandwidths could be comparable to the. The main advantage of the RF-SET readout voltage noise, since high-quality field-effect attain  $\sim \text{nV}/\sqrt{\text{Hz}}$ . The bandwidth of a due to their 1,000 times higher capacitance greater than about a hundred hertz for the impedance of the SIS detector. In addition dissipation and operating temperature to simplify the scaling to a large number of channels. Si FET's must be kept at 100 K, an implement with 100 mK detectors in large

## VI. FABRICATION AND INITIAL

Several integrated devices of the design have been fabricated in the Swedish Nanofactory, and an electron micrograph of one of detectors is shown in Figure 2. The fabrication included several steps of direct-write lithography and thermal evaporation. First, the contacts were deposited. The Al absorber (of  $16 \Omega$ ), detector junctions, and SET are in the next lithography step. The SET detail B) were made using a standard deposition technique through this resist pattern area of approximately  $80 \times 80 \text{ nm}$ , capacitance of approximately  $0.2 \text{ fF}$  per junction, and resistance  $\sim 50 \Omega$ . The absorber strip was also fabricated at the same time as the detector junction made during the same lithography step. Finally, the Pb bowtie antenna layer was deposited over the absorber. Low resistance contacts from absorber to antenna were made through small gaps in the absorber. All of the elements were electrically functioning.

The detector junction was actually (see Figure 2) split into two separate junctions, each of about  $100 \times 300 \text{ nm}$ . Separate counter-propagating detector junctions are extended to form a SQUID loop with an area of several square micrometers. The two junctions thus form a SQUID, which allows for the supercurrent of the parallel combination with a magnetic field of only a few Gauss to depress the superconducting gaps. The critical current of the junction combination had an  $R_N$  of  $1 \text{ k}\Omega$ , (at  $T = 50 \text{ mK}$ ) is shown in Figure 3. The subgap current are taken with for two magnetic fields, and demonstrates the presence of supercurrent. The bottom trace in Figure 3 shows the modulation of the SET with the voltage gate, and allows determination of the gate capacitance  $C_{gate} = 0.55 \text{ fF}$ .

The subgap current of this first device is about 100 times smaller than the normal-state current.

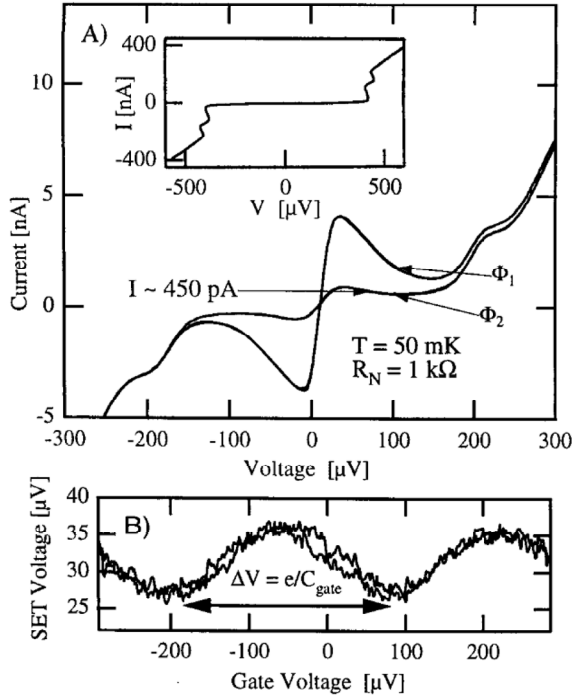


Fig. 3. Data from dc characterization of device such as that shown in Figure 2. A) Current-voltage characteristic of double-junction SIS detectors, for two different values of applied magnetic field. Inset shows I-V on larger scale. B) Response of integrated SET to voltage applied to the input gate. The observed periodicity allows a determination of the gate capacitance,  $C_{gate} = 0.54$  fF.

in this first characterization the influence of external noise or stray light cannot be ruled out. The junctions also displayed some non-ideal behavior, which could be due to nonequilibrium effects from the wiring layers, or bad alignment. Even this relatively high leakage current should yield a very sensitive detector, however. The expected sensitivity, given the measured dc characteristics, is detailed in Table 1, and would be at the state-of-the-art for direct detectors, with an NEP of a few  $10^{-18}$  W/ $\sqrt{\text{Hz}}$ . Future designs for true photon counting will have to investigate the leakage current and minimize it, as well as reduce the parasitic capacitance to allow high speed operation.

## VII. SUMMARY

In conclusion, we have presented the concept for and demonstrated the fabrication of a combined superconducting/single-electron device which can serve as a far-IR direct detector with sensitivities as much as 100 times better than present state-of-the-art bolometers, and response times of less than  $1 \mu\text{s}$ . Furthermore, this SQPC is in essence a photoconductor, rather than a thermal (bolometric) detector. When comparing a device which utilizes a bandgap against a true bolometer, the simple expectation is that the performance will increase more rapidly (dark current should scale exponentially) with a

decrease in operating temperature than in the detector. Initial devices which incorporate an readout using a fast RF-SET have been fabricated even these unoptimized designs should give NEP  $10^{-18}$  W/ $\sqrt{\text{Hz}}$ . Eventually, devices of this type should approach  $10^{-20}$  W/ $\sqrt{\text{Hz}}$ , and even yield a true sin counter in the submillimeter band.

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